



TECHNISCHE  
UNIVERSITÄT  
DRESDEN

# SEMINAR SELECTED TOPICS IN DATABASE THEORY

## **Lecture 1: Introduction / The Relational Model**

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Knowledge-Based Systems

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# Introduction

# Course Tutors



David Carral



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# Structure of the Seminar and Evaluation

## Lectures

- **Wednesday 10th (i.e., today), DS6:** Introductory lecture 1
- **Wednesday 17th, DS6:** Introductory lecture 2
- **Afterwards:** Office hours in 3035 and presentations

## Evaluation

- **Paper summary:** self-selected research paper;<sup>a</sup> ~15 pages
- **Presentation:**
  - 20 minutes + discussion
  - Participate in the presentations of other students

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<sup>a</sup>See the “Literature” tab at [https://iccl.inf.tu-dresden.de/web/Research\\_Advances\\_in\\_Database\\_Theory\\_\(WS2018\)](https://iccl.inf.tu-dresden.de/web/Research_Advances_in_Database_Theory_(WS2018)).

## Other stuff...

### Web Page

[https://iccl.inf.tu-dresden.de/web/Research\\_Advances\\_in\\_Database\\_Theory\\_\(WS2018\)](https://iccl.inf.tu-dresden.de/web/Research_Advances_in_Database_Theory_(WS2018))

### Lecture Notes

All slides will be available online.

### Reading list

Serge Abiteboul, Richard Hull, Victor Vianu; **Foundations of databases**. Available at <http://webdam.inria.fr/Alice/>

### Acknowledgements

Check out Vim Martens!

On to the content...

# What is a database?

A **Database Management System** (DBMS) is a software to manage collections of data. The **architecture of DBMS** consist of three levels:

- **External Level:** Application-specific user views
- **Logical Level:** Abstract data model, independent of implementation, conceptual view
- **Physical Level:** Data structures and algorithms, platform-specific

**In this seminar:** focus on logical view for relational data model

# The Relational Model



Database = collection of tables

## Schedule

Movie	Cinema	Date	R-rated
Goodfellas	Thalia	15/10	True
Unforgiven	Thalia	17/10	True
Boogie Nights	Rundkino	21/11	True
Annie Hall	Rundkino	21/11	False

A table has a **schema**:

- Schedule[{Movie, Cinema, Date, R-rated}]

# Towards a formal definition of “table”

A table row has one value for each column.

- That is, a row is a function from the attributes of the table schema to specific values.

## Schedule

Movie	Cinema	Date	R-rated
...	...	...	...
Boogie Nights	Rundkino	21/11	True
...	...	...	...

The above row can be represented with the function:

$$f : \{\mathbf{Movie} \mapsto \text{Boogie Nights}, \mathbf{Cinema} \mapsto \text{Rundkino}, \\ \mathbf{Date} \mapsto \text{21/11}, \mathbf{R-rated} \mapsto \text{True}\}$$

# Database = set of tables

Let **dom** (“domain”) be the set of conceivable values in tables.

## Definition 1

- A **relation schema**  $R[U]$  consists of a relation name  $R$  and a finite set  $U$  of attributes
- $|U|$  is the arity of  $R[U]$
- A **table** for  $R[U]$  is a finite set of functions from  $U$  to **dom**
- A **database instance**  $\mathcal{I}$  is a finite set of tables

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**Note:** we disregard the order and multiplicity of rows.

Tables are also called relation instances. The table with relation schema  $R[U]$  in the database instance  $\mathcal{I}$  is written  $R^{\mathcal{I}}$ .

# Database = set of tables

## Schedule

Movie	Cinema	Date	R-rated
Goodfellas	Thalia	15/10	True
Unforgiven	Thalia	17/10	True
Boogie Nights	Rundkino	21/11	True
Annie Hall	Rundkino	21/11	False

- The domain **dom** of the above table is the following set:  
{Goodfellas, Thalia, 15/10, True, Unforgiven, Thalia, 17/10, Boogie Nights, Rundkino, 21/11, Annie Hall, Rundkino, False }
- The above is a table for the relation schema Schedules[**{Movie, Cinema, Date, R-rated}**]
- Let  $\mathcal{I}$  be a database instance. Then, Schedules $^{\mathcal{I}}$  is the set of rows in this table.

# Database = set of tables

## Schedule

Movie	Cinema	Date	R-rated
Goodfellas	Thalia	15/10	True
Unforgiven	Thalia	17/10	True
Boogie Nights	Rundkino	21/11	True
Annie Hall	Rundkino	21/11	False

The table represented above is the set  $\{r_1, r_2, r_3, r_4\}$  where  $r_1, r_2, r_3$ , and  $r_4$  are the following functions:

$$r_1 = \{\mathbf{M} \mapsto \text{Goodfellas}, \mathbf{C} \mapsto \text{Thalia}, \mathbf{D} \mapsto 15/10, \mathbf{R} \mapsto \text{True}\}$$

$$r_2 = \{\mathbf{M} \mapsto \text{Unforgiven}, \mathbf{C} \mapsto \text{Thalia}, \mathbf{D} \mapsto 17/10, \mathbf{R} \mapsto \text{True}\}$$

$$r_3 = \{\mathbf{M} \mapsto \text{Boogie Nights}, \mathbf{C} \mapsto \text{Rundkino}, \mathbf{D} \mapsto 21/11, \mathbf{R} \mapsto \text{True}\}$$

$$r_4 = \{\mathbf{M} \mapsto \text{Annie Hall}, \mathbf{C} \mapsto \text{Rundkino}, \mathbf{D} \mapsto 21/11, \mathbf{R} \mapsto \text{False}\}$$

# Database = set of relations

**Remark:** Attribute names do not matter. Instead of the function

$\{\mathbf{M} \mapsto \text{Goodfellas}, \mathbf{C} \mapsto \text{Thalia}, \mathbf{D} \mapsto 15/10, \mathbf{R} \mapsto \text{True}\}$

we could also use a tuple:

$\langle \text{Goodfellas}, \text{Thalia}, 15/10, \text{True} \rangle$

**Necessary assumption:** Attributes have a fixed order.

## Definition 2

- A **relation schema**  $R[U]$  is defined as before
- A **table** for  $R[U]$  is a finite subset of  $\mathbf{dom}^{|U|}$
- A **database instance**  $\mathcal{I}$  is a finite set of tables

# Database = set of relations

## Schedule

<b>Movie</b>	<b>Cinema</b>	<b>Date</b>	<b>R-rated</b>
Goodfellas	Thalia	15/10	True
Unforgiven	Thalia	17/10	True
Boogie Nights	Rundkino	21/11	True
Annie Hall	Rundkino	21/11	False

The table represented above is the following set:

$\{ \langle \text{Goodfellas}, 15/10, \text{True}, \text{Thalia} \rangle, \langle \text{Unforgiven}, 17/10, \text{True}, \text{Thalia} \rangle, \langle \text{Boogie Nights}, 21/11, \text{True}, \text{Rundkino} \rangle, \langle \text{Annie Hall}, 21/11, \text{False}, \text{Rundkino} \rangle \}$



# Database = set of facts

Another convenient way to write databases:

## Definition 3

A **fact** is an expression  $p(t_1, \dots, t_n)$  where

- $p$  is an  $n$ -ary predicate symbol
- $t_1, \dots, t_n$  are constant symbols

A **database instance** is a finite set of facts.

Database = set of facts

## Schedule

<b>Movie</b>	<b>Cinema</b>	<b>Date</b>	<b>R-rated</b>
Goodfellas	Thalia	15/10	True
Unforgiven	Thalia	17/10	True
Boogie Nights	Rundkino	21/11	True
Annie Hall	Rundkino	21/11	False

The information in the above corresponds to the following facts:

Schedule(Goodfellas, 15/10, True, Thalia)

Schedule(Unforgiven, 17/10, True, Thalia)

Schedule(Boogie Nights, 21/11, True, Rundkino)

Schedule(Annie Hall, 21/11, False, Rundkino)

# Graphical Representation

Director(Scorsese)

DirectedBy(Goodfellas, Scorsese)

ActsIn(De Niro, Goodfellas)

ActsIn(Pesci, Goodfellas)



# Summary: Different Perspectives

<b>Perspective</b>	<b>DB Instance</b>	<b>Table</b>	<b>Row</b>
Named	Set of tables	Set of functions	Function
Unnamed	Set of tables	Set of tuples	Tuple
Fact-based	Set of facts	Set of facts	Fact
Graph	Labelled hypergraph	L. hypergraph	L. Edge

# The Relational Algebra

# Relational Algebra Queries

Query language based on a set of **operations** on databases.  
Each operation refers to some tables and produces another table.

Main operations of the named perspective:

- Selection  $\sigma$
- Projection  $\pi$
- Join  $\bowtie$
- Renaming  $\delta$
- Difference  $-$
- Union  $\cup$
- Intersection  $\cap$

# Selection

“Find all R-rated movies”

$\sigma_{R\text{-rated}=\text{“True”}}$  Schedule

“Find all connections that begin and end in the same stop”

$\sigma_{\text{From}=\text{to}}$  Connect

## Definition 4

The **selection operator** has the form  $\sigma_{n=m}$

- $n$  is an attribute name
- $m$  is an attribute name or a constant value

Consider a table  $R^I$  for the relational schema  $R[U]$ .

- For  $m$  constant value:  $\sigma_{n=m}(R^I) = \{f \in R^I \mid f(n) = m\}$
- For  $m$  attribute name:  $\sigma_{n=m}(R^I) = \{f \in R^I \mid f(n) = f(m)\}$

# Selection

“Find all dates in which some movie is projected.”

$\pi_{\text{Date}}$  Schedule

## Definition 5

The **projection operator** has the form  $\pi_{a_1, \dots, a_n}$  where each  $a_i$  is an attribute name.

Consider a table  $R^I$  for  $R[U]$ .

$$\pi_{a_1, \dots, a_n}(R^I) = \{f_{\{a_1, \dots, a_n\}} \mid f \in R^I\}$$

where  $f_{\{a_1, \dots, a_n\}}$  is the restriction of  $f$  to the domain  $\{a_1, \dots, a_n\}$ , i.e., the function  $\{a_1 \mapsto f(a_1), \dots, a_n \mapsto f(a_n)\}$ .

**Remark:** Projection is only defined if  $a_i \in U$  for each  $a_i$ .



# Natural Join

## Schedule

Movie	Cinema	Date	R-rated
Unforgiven	Thalia	17/10	True
Boogie Nights	Rundkino	21/11	True

## Location

Cinema	Neighborhood
Thalia	Neudstadt
Rundkino	Altstadt

## Schedule $\bowtie$ Location

Movie	Cinema	Date	R-rated	Neighborhood
Unforgiven	Thalia	17/10	True	Neudstadt
Boogie Nights	Rundkino	21/11	True	Altstadt

# Natural Join

## Definition 6

The **natural join** operator has the form  $\bowtie$ .

Consider tables  $R^I$  for  $R[U]$  and  $S^I$  for  $S[V]$ .

$$R^I \bowtie S^I = \{f : U \cup V \rightarrow \mathbf{dom} \mid f_U \in R^I \text{ and } f_V \in S^I\}$$

where  $f_U$  (resp.  $f_V$ ) is the restriction of  $f$  to elements in  $U$  (resp.  $V$ ) as before.

# Rename

$\delta_{\text{Movie, Cinema, Date, R-rated} \rightarrow \text{Film, Cinema, Date, R-rated}}$  (Schedule)

## Definition 7

The **renaming operator** has the form  $\delta_{a_1, \dots, a_n \rightarrow b_1, \dots, b_n}$  with all  $a_i$  mutually distinct attribute names, and likewise for all  $b_i$ .

Consider a table  $R^I$  for  $R[\{a_1, \dots, a_n\}]$

$$\delta_{a_1, \dots, a_n \rightarrow b_1, \dots, b_n}(R^I) = \{f \circ g \mid f \in R^I \text{ and } g : \{b_i \mapsto a_i\}_{1 \leq i \leq n}\}$$

where  $f \circ g$  is function composition:  $(f \circ g)(x) = f(g(x))$

# Difference, Union, Intersection

- Binary operators defined like the usual set operations.
- **Remark:** These operators are only defined on tables of the same relational schema. That is, tables with the same set of attributes.

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  - Studying combined/data/query Complexity.

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  - Fragments of relational algebra such as **conjunctive queries**. That is, relational algebra expressions that use only select, project, join, and rename.
  - Extensions of relational algebra such as **Datalog**.

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- Study the “expressivity” of a query language.
  - Let’s do this!