

Deduction Systems

Tutorial 2

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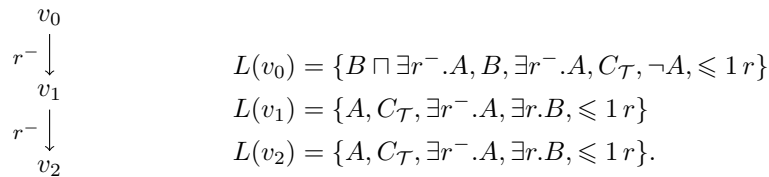
Exercise 2.1. Transform the following concepts into negation normal form:

- (a) $\neg(A \sqcap \forall r.B)$
- (b) $\neg\forall r.\exists s.(\neg B \sqcup \exists r.A)$
- (c) $\neg((\neg A \sqcap \exists r.\top) \sqcup \geq 3 s.(A \sqcup \neg B))$

Exercise 2.2. Apply the tableau algorithm in order to check if the axiom $A \sqsubseteq B$ is a logical consequence of the TBox $\{\neg C \sqsubseteq B, A \sqcap C \sqsubseteq \perp\}$.

Exercise 2.3. Apply the tableau algorithm in order to check satisfiability of the concept $A \sqcap \forall r.B$ w.r.t. the TBox $\{A \sqsubseteq \exists r.A, B \sqsubseteq \exists r^-.C, C \sqsubseteq \forall r.\forall r.B\}$.

Exercise 2.4. Lukas wants to apply the tableau algorithm for checking the satisfiability of the concept $B \sqcap \exists r^-.A$ w.r.t. the TBox $\{A \sqsubseteq \exists r^-.A \sqcap \exists r.B, \top \sqsubseteq \leq 1 r\}$. He arrives at the situation depicted below and concludes that no further rules are applicable, since v_2 is blocked by v_1 . What is Lukas' error? Continue the algorithm until its termination. (You don't have to illustrate all intermediate steps, just provide the final state.)



Exercise 2.5. Extend the ≤ 1 rule in a way that also qualified functionality axioms of the form $\top \sqsubseteq \leq 1 r.A$ can be treated correctly, where A is an atomic concept. Can you also treat arbitrary axioms of the form $C \sqsubseteq \leq 1 r.D$?