

# Foundations of Constraint Programming

## Tutorial 1 (on October 21st)

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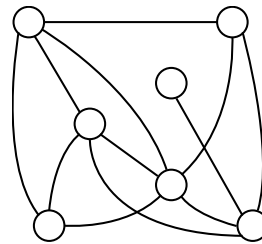
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**Exercise 1.1:**

Consider the task of assigning to each node of a finite graph a color in such a way that no two adjacent nodes have the same color. Such an assignment is called a *coloring* of the graph. Formulate the problem of given only 3-colors as constraint satisfaction problem.

**Exercise 1.2:**

Consider the depicted graph (to the right), consisting of 7 nodes to which the numbers  $1, \dots, 7$  must be assigned. Each of the nodes has at least one neighbor, whereas the sum of all neighbors of a node must be the sum given in the following table. E.g. if 3 is the assigned node value, then its neighbors must sum up to 14.



<i>node value</i>	1	2	3	4	5	6	7
	=	=	=	=	=	=	=
<i>sum of its neighbors</i>	20	18	14	19	2	7	8

Formulate the riddle as CSP.

**Exercise 1.3:**

A coloring of a graph involving the minimal number of colors is called the *chromatic number* of the graph. Formulate the problem of finding the chromatic number of a graph as a constrained optimization problem.

**Exercise 1.4:**

Formulate the following problem as a constrained optimization problem: Place a minimum number of queens on the chess board so that each unoccupied field comes under attack.