

Exercise Sheet 1: Getting to Know Graphs

Larry González, Markus Krötzsch
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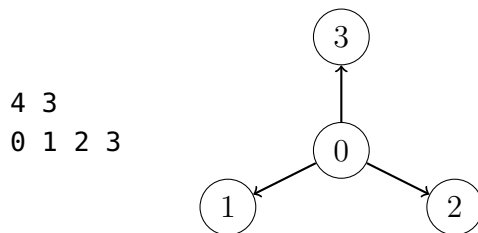
Exercise 1.1. Show that the number of vertices of odd degree is even in every simple graph.

Exercise 1.2. Write a program that reads a directed graph from a file in the format of Exercise 0.2 and prints out the graph in METIS graph format:

n	m			
v_1	n_1^1	n_1^2	\dots	$n_1^{d_1}$
v_2	n_2^1	n_2^2	\dots	$n_2^{d_2}$
\vdots	\vdots	\vdots	\dots	\vdots
v_n	n_n^1	n_n^2	\dots	$n_n^{d_n}$

The first line consists of two integers n and m , separated by a space, where n is the number of vertices, and m is the total number of edges. Each of the following lines specifies the neighbours $n_i^1, n_i^2, \dots, n_i^{d_i}$ of vertex v_i .

As an example, the directed star S_3 would be encoded as:



We use the same data from previous exercise. Data files are available at <https://github.com/knowsys/Course-Knowledge-Graphs/tree/master/exercises/00-introduction-to-python/data>.

Exercise 1.3. A triangle in a directed graph is a simple directed path $v_1 \xrightarrow{e_1} v_2 \xrightarrow{e_2} v_3 \xrightarrow{e_3} v_1$.

Write a program that reads a directed graph G from a file in the format of Exercise 0.2 and prints out the number of triangles in G . How does the runtime of your program scale with the size of the input graph?

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* **Exercise 1.4.** Let $G = \langle V, E \rangle$ be an undirected graph. Show that if G is triangle-free (i.e., there are no triangles in G), then

$$|E| \leq \left\lfloor \frac{|V|^2}{4} \right\rfloor.$$