

Evaluating the Generality of Disjunctive Model Faithful Acyclicity on OWL ontologies

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Disjunctive Existential Rules

$$\forall \vec{x} \forall \vec{y}. \text{Body}(\vec{x}, \vec{y}) \rightarrow \bigvee_{i=1}^n \exists \vec{z}_i. \text{Head}^i(\vec{x}_i, \vec{z}_i)$$

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- *Body* and *Head*^{*i*}: conjunctions of atoms
- $\vec{x}, \vec{y}, \vec{z}_i$: pairwise disjoint lists of variables
- $\bigcup_{i=1}^n \vec{x}_i = \vec{x}$

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Disjunctive Skolem Chase

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- $\text{somePizza} : \text{Pizza}$

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Disjunctive Skolem Chase

$\text{SalamiPizza}(x) \rightarrow \text{hasBase}(x, f^z(x)) \wedge \text{CheesePizza}(f^z(x))$

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● $somePizza : Pizza, CheesePizza$

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$hasBase$ → ● $f^z(somePizza) : CheesePizza, Pizza$

The *disjunctive skolem chase* yields a *universal model set*.

Acyclicity Notions

Problem: Termination of the chase is undecidable.
Sufficient conditions for termination have been introduced.

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Disjunctive Existential Rule Sets	
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General Idea: Compute the chase on a *critical instance* using only rules that are not *blocked*.

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$\text{hasBase} \begin{array}{c} \circlearrowleft \\ \bullet \end{array} \star : \text{Pizza}, \text{CheesePizza}, \text{SalamiPizza}$

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The **second rule** is blocked now.
The rule set is DMFA since the computed fact set has no *cyclic terms*.

Evaluation Outline

Datasets:

- Oxford ontology repository (OXFD)
797 ontologies¹
- OWL Reasoner Evaluation 2015 (ORE15)
1920 ontologies²

Steps:

¹OXFD - <https://www.cs.ox.ac.uk/isg/ontologies/>

²ORE15 - <https://zenodo.org/record/18578>

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SalamiPizza $\sqsubseteq \geq 1$ *hasBase.CheesePizza*
Pizza \sqsubseteq *CheesePizza* \sqcup *SalamiPizza*
CheesePizza \sqsubseteq *Pizza*

Steps:

1. Normalize Ontologies using an existing tool³

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$SalamiPizza \sqsubseteq \geq 1 hasBase.CheesePizza$
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$SalamiPizza(x) \rightarrow \exists z.hasBase(x, z) \wedge CheesePizza(z)$
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3. Check MFA, DMFA, and RMFA⁵

$\text{SalamiPizza} \sqsubseteq \geq 1 \text{hasBase.CheesePizza}$
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not MFA but DMFA and RMFA

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Translation of normalized Axioms

$$A_1 \sqcap \dots \sqcap A_n \sqsubseteq B \qquad A_1(x) \wedge \dots \wedge A_n(x) \rightarrow B(x) \qquad (1)$$

Here, $A, A_1, \dots, A_n, B, B_1, \dots, B_{n'}$ are classes, R, R_1, \dots, R_k, S are (inverse) properties, a_1, \dots, a_l are individuals, and m, m' are integers ≥ 0 .

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$$A \sqsubseteq \forall R.B \qquad A(x) \wedge R(x, y) \rightarrow B(y) \qquad (3)$$

$$A \sqsubseteq \geq m R.B \qquad (\text{more involved}) \qquad (4)$$

$$A \sqsubseteq \leq m' R.B \qquad (\text{more involved}) \qquad (5)$$

$$A \sqsubseteq \{ a_1, \dots, a_l \} \qquad (\text{more involved}) \qquad (6)$$

$$R_1 \circ \dots \circ R_k \sqsubseteq S \qquad R_1(x_1, x_2) \wedge \dots \wedge R_k(x_k, x_{k+1}) \rightarrow S(x_1, x_{k+1}) \qquad (7)$$

$$R \sqcap S \sqsubseteq \perp \qquad R(x, y) \wedge S(x, y) \rightarrow \perp \qquad (8)$$

$$A \sqsubseteq \exists R.\text{Self} \qquad A(x) \rightarrow R(x, x) \qquad (9)$$

$$\exists R.\text{Self} \sqsubseteq A \qquad R(x, x) \rightarrow A(x) \qquad (10)$$

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Complicated Axioms

The translation for $A \sqsubseteq \geq 2R.B$ is more involved:

$$\begin{array}{lll} A(x) \rightarrow \exists z_1.R_1(x, z_1) \wedge B(z_1) & R_1(x, y) \rightarrow R(x, y) & R(x, y) \rightarrow R_1(x, y) \vee R_2(x, y) \\ A(x) \rightarrow \exists z_2.R_2(x, z_2) \wedge B(z_2) & R_2(x, y) \rightarrow R(x, y) & R_1(x, y) \wedge R_2(x, y) \rightarrow \perp \end{array}$$

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For $A \sqsubseteq \leq 1R.B$ and $A \sqsubseteq \{a, b\}$, we require equality:

$$A(x) \wedge R(x, u) \wedge B(u) \wedge R(x, v) \wedge B(v) \rightarrow u = v \qquad A(x) \rightarrow x = a \vee x = b$$

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Problem: DMFA does not support equality.

For now: Omit axioms that require equality.

Later on: Axiomatize equality as suggested in [Carral and Urbani, 2020].

DMFA Implementation

Input: Ruleset R

Output: Is R DMFA?

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- 4 **while** $\Delta F \neq \emptyset$ **do**

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    // keeps track of already computed facts internally
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9   end
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Evaluation Results

OXFD: 797
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OXFD: 797 Normalization 791
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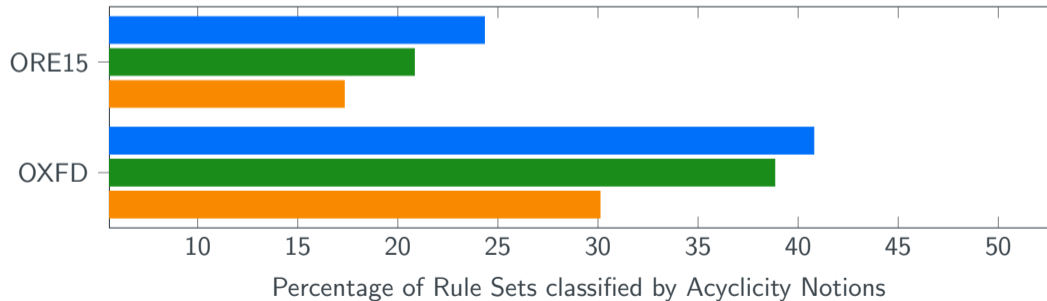
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MFA DMFA RMFA



Where are the differences?

Observation: 6 out of 9 rule sets for OXFD and 11 out of 18 rule sets for ORE15 that are DMFA but not MFA come from BioPAX.⁶

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We have to be careful in generalizing our findings here.

OXFD 00007: DMFA but not MFA

$Evidence(x) \rightarrow \exists z. ConfidenceProp(x, z)$

$ConfidenceProp(x, y) \rightarrow Confidence(y)$

$Confidence(x) \rightarrow Xref(x)$

$Xref(x) \rightarrow Evidence(x) \vee Confidence(x)$

$Evidence(x) \wedge Confidence(x) \rightarrow \perp$

⁶BioPAX - <http://www.biopax.org/>

Where are the differences?

Observation: 6 out of 9 rule sets for OXFD and 11 out of 18 rule sets for ORE15 that are DMFA but not MFA come from BioPAX.⁶
They are similar or even identical.

We have to be careful in generalizing our findings here.

OXFD 00007: DMFA but not MFA

$Evidence(x) \rightarrow \exists z. ConfidenceProp(x, z)$

$ConfidenceProp(x, y) \rightarrow Confidence(y)$

$Confidence(x) \rightarrow Xref(x)$

$Xref(x) \rightarrow Evidence(x) \vee Confidence(x)$

$Evidence(x) \wedge Confidence(x) \rightarrow \perp$

OXFD 00114: RMFA but not DMFA

$Sibling(x) \rightarrow \exists z. hasSibling(z, x) \wedge Person(z)$

$Person(x) \wedge hasSibling(x, y) \rightarrow Sibling(y)$

$Sibling(x) \rightarrow Person(x)$

$hasSibling(x, y) \rightarrow hasSibling(y, x)$

Not even terminating w.r.t. the disjunctive skolem chase.

⁶BioPAX - <http://www.biopax.org/>

Second Example in Detail

Sibling(x) → ∃z.hasSibling(z, x) ∧ Person(z)

Person(x) ∧ hasSibling(x, y) → Sibling(y)

Sibling(x) → Person(x)

hasSibling(x, y) → hasSibling(y, x)

Second Example in Detail

Sibling(x) $\rightarrow \exists z. hasSibling(z, x) \wedge Person(z)$

Person(x) $\wedge hasSibling(x, y) \rightarrow Sibling(y)$

Sibling(x) $\rightarrow Person(x)$

hasSibling(x, y) $\rightarrow hasSibling(y, x)$

me : *Sibling*



Second Example in Detail

$Sibling(x) \rightarrow \exists z. hasSibling(z, x) \wedge Person(z)$

$Person(x) \wedge hasSibling(x, y) \rightarrow Sibling(y)$

$Sibling(x) \rightarrow Person(x)$

$hasSibling(x, y) \rightarrow hasSibling(y, x)$

$me : Sibling, Person \bullet$

Second Example in Detail

$Sibling(x) \rightarrow \exists z. hasSibling(z, x) \wedge Person(z)$

$Person(x) \wedge hasSibling(x, y) \rightarrow Sibling(y)$

$Sibling(x) \rightarrow Person(x)$

$hasSibling(x, y) \rightarrow hasSibling(y, x)$

$me : Sibling, Person$ ●

$hasSibling$ ● $f^z(me) : Person$



Second Example in Detail

$Sibling(x) \rightarrow \exists z. hasSibling(z, x) \wedge Person(z)$

$Person(x) \wedge hasSibling(x, y) \rightarrow Sibling(y)$

$Sibling(x) \rightarrow Person(x)$

$hasSibling(x, y) \rightarrow hasSibling(y, x)$



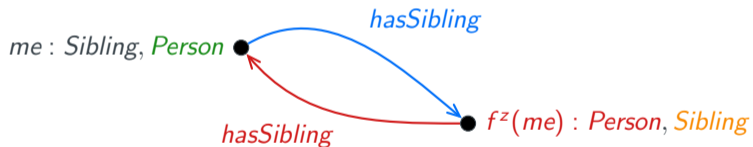
Second Example in Detail

$Sibling(x) \rightarrow \exists z. hasSibling(z, x) \wedge Person(z)$

$Person(x) \wedge hasSibling(x, y) \rightarrow Sibling(y)$

$Sibling(x) \rightarrow Person(x)$

$hasSibling(x, y) \rightarrow hasSibling(y, x)$



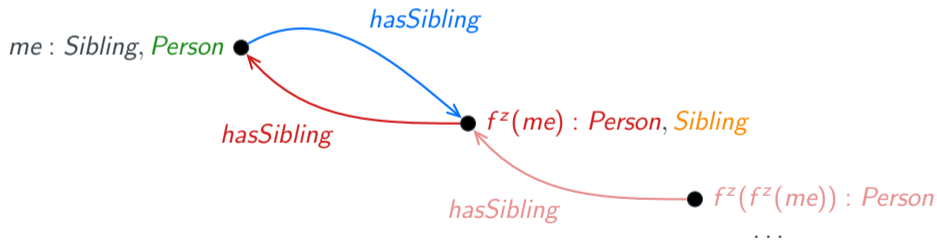
Second Example in Detail

$Sibling(x) \rightarrow \exists z. hasSibling(z, x) \wedge Person(z)$

$Person(x) \wedge hasSibling(x, y) \rightarrow Sibling(y)$

$Sibling(x) \rightarrow Person(x)$

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Conclusion

Results:

- DMFA improves upon MFA and comes closer to RMFA in practice.
- A significant number of rule sets is not even RMFA.
- We find rule sets that are RMFA but not DMFA that do not terminate w.r.t. the disjunctive skolem chase.

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Open Questions:

- What is the impact of the translation (especially equality) on the results?
- How tight is DMFA?

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Open Questions:

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Future Work:

- Handling for equality in the translation.
- Investigation and evaluation of cyclicity notions for the disjunctive skolem chase.
- Performance centric evaluation of DMFA.
- Implementation of the disjunctive skolem chase, e.g. with ASP solvers with lazy grounding.




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