

Foundations of Logic Programming

Tutorial 4 (on December 15th)

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Exercise 5.1:

Consider the following program \mathcal{P} :

$$\begin{aligned} & p(X, X, c). \\ & p(f(X), Y, f(Z)) \text{ :- } p(X, Y, Z). \end{aligned}$$

- Indicate the Herbrand universe HU_F and the Herbrand base $HB_{\Pi, F}$ determined by \mathcal{P} .
- Give the least Herbrand model \mathcal{I}_1 of \mathcal{P} .
- Give a Herbrand model \mathcal{I}_2 of \mathcal{P} , different from \mathcal{I}_1 .
- Give a classical model model \mathcal{I}_3 of \mathcal{P} , different from \mathcal{I}_1 and \mathcal{I}_2 .

Exercise 5.2:

Take the following program P :

$$\begin{aligned} & p \leftarrow . \\ & p \leftarrow p. \\ & q \leftarrow r. \\ & q \leftarrow \neg r, p. \\ & r \leftarrow \neg p. \\ & t \leftarrow q. \\ & t \leftarrow r, \neg q. \end{aligned}$$

- Construct the dependency graph D_P of P .
- Is P stratified and/or hierarchical?
- Give a stratification of P .
- Using your stratification to show how to compute the standard model M_P of P .

Exercise 5.3:

Consider the following program:

$$\begin{aligned}p(X) &\leftarrow r([a|X]) \\r([Y|X]) &\leftarrow s(X) \\s([Y|X]) &\leftarrow p(X)\end{aligned}$$

- a) Provide a level mapping for which the program is recurrent.
- b) Provide a bounded query for this level mapping which contains at least one variable.
- c) Provide an unbounded query for this level mapping.