



Knowledge Graphs

Lecture 7: Datalog for Knowledge Graphs

Markus Krötzsch Knowledge-Based Systems

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More recent versions of this slide deck might be available.

For the most current version of this course, see

https://iccl.inf.tu-dresden.de/web/Knowledge_Graph

Review

Semantics of each feature is defined by specific algebra operators

- $\mathsf{Join}(M_1, M_2)$: join compatible mappings from M_1 and M_2
- Filter $_G(\varphi, M)$: remove from multiset M all mappings for which φ does not evaluate to EBV "true"
- Union (M_1, M_2) : compute the union of mappings from multisets M_1 and M_2
- Minus (M_1, M_2) : remove from multiset M_1 all mappings compatible with a non-empty mapping in M_2
- LeftJoin $_G(M_1, M_2, \varphi)$: extend mappings from M_1 by compatible mappings from M_2 when filter condition is satisfied; keep remaining mappings from M_1 unchanged
- Extend (M, v, φ) : extend all mappings from M by assigning v the value of φ .
- OrderBy(L, condition): sort list by a condition
- Slice(L, start, length): apply limit and offset modifiers

Further operators exist, e.g., Distinct(L).

Translating SPARQL to nested algebra expressions is mostly straightforward (we saw an algorithm for a subset of features).

Introduction to Datalog

The Simplest Rule Language

 $hasUncle(x, z) \leftarrow hasParent(x, y), hasBrother(y, z)$

The Simplest Rule Language

$$hasUncle(x, z) \leftarrow hasParent(x, y), hasBrother(y, z)$$

Some terminology:

- terms can be variables (e.g., x, y, z) or constants
- predicates denote relations; they have an arity (e.g., hasUncle has arity 2)
- atoms are constructed from predicates and terms (e.g., hasUncle(x, z))

Definition 7.1: A Datalog rule is an expression of the form:

$$H \leftarrow B_1, \ldots, B_m$$

where H and B_1, \ldots, B_m are atoms. H is called the head or conclusion; B_1, \ldots, B_m is called the body or premise. A rule with empty body (m=0) is called a fact. A ground rule is one without variables (i.e., all terms are constants).

Datalog Syntax in the Wild

In contrast to SPARQL and RDF, Datalog is not a standard . . .

Top to bottom: Prolog/ASP, Soufflé, Nemo, RDFox, Logica, Datomic, Percial, N3

From Rules to Programs

Example:

```
father(alice, bob)
 mother(alice, cho)
 father(cho, daniel)
 mother(cho, eiko)
mother(finley, eiko)
         parent(x, y) \leftarrow father(x, y)
         parent(x, y) \leftarrow mother(x, y)
      ancestor(x, y) \leftarrow parent(x, y)
      ancestor(x, z) \leftarrow ancestor(x, y), parent(y, z)
    commonAnc(x) \leftarrow ancestor(alice, x), ancestor(finley, x)
```

Trying it out

We will use Nemo for hands-on exercises.



Web app: https://tools.iccl.inf.tu-dresden.de/nemo/

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Task: Define an auncle (aunt or uncle) relation.

Hint: You might need inequality !=.

Nemo is free and open source. Issue reports and feature requests are welcome.

Datalog Programs as Functions

Idea:

Datalog programs represent functions from sets of input facts and to sets of output facts.

Definition 7.2: A Datalog program is a triple $\langle P, P_{in}, P_{out} \rangle$, where

- P is a finite set of rules,
- P_{in} is a non-empty set of input predicates that do not occur in rule heads of P, and
- Pout is a non-empty set of output predicates.

We require all predicates in P_{in} and P_{out} to occur in P.

Input predicates are also called EDB predicates, and all other (non-input) predicates are also called IDB predicates.

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Input predicates are also called EDB predicates, and all other (non-input) predicates are also called IDB predicates.

Note 1: Normally we want input facts to change, not to be a static part of programs.

Note 2: Finite sets of facts are often called databases, so Datalog maps input databases to output databases.

A Datalog Program

```
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 mother(alice, cho)
 father(cho, daniel)
 mother(cho, eiko)
mother(finley, eiko)
         parent(x, y) \leftarrow father(x, y)
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```

Input (=EDB) predicates: father, mother

Output predicates: commonAnc

IDB predicates: parent, ancestor, commonAnc

An Equivalent Datalog Program

```
father(alice, bob)
 mother(alice, cho)
 father(cho, daniel)
 mother(cho, eiko)
mother(finley, eiko)
      ancestor(x, y) \leftarrow father(x, y)
      ancestor(x, y) \leftarrow mother(x, y)
      ancestor(x, z) \leftarrow ancestor(x, y), ancestor(y, z)
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- Verifiability and Certifiability: Correctness can be proven independently
- Intuitive Understandability: Logic capturing natural human thinking (questionable claim)
- Conciseness and Fast Development: Programs can focus on essentials of task at hand; program logic independent of underlying data structures
- → Could mostly be said about SPARQL as well ...
 but Datalog use cases are often hard or impossible to address with SPARQL

What is it good for? (1)

Application Area 1: Rule-Based Knowledge Representation and Reasoning

Datalog-like rules occur in many applications of formal logic:

- Direct use of rules in many reasoning approaches (e.g., qualitative spatial reasoning)
- Many logics admit Datalog-based reasoning mechanisms (e.g., reasoning for OWL EL ontologies)
- Sometimes reasoning subtasks can be outsourced to Datalog (e.g., grounding in ASP, unit propagation in theorem proving)

Typical system requirements:

- Fast, reactive systems; typically main-memory based
- Pure Datalog, limited need for extensions

What is it good for? (2)

Application Area 2: Analysis of Structured Data

Datalog is great for analysing structured data, especially with nested/recursive structures:

- Program analysis (e.g., CodeQuest)
- Data flow and control flow analysis (e.g., DOOP/Soufflé)
- HTML analysis and data extraction (e.g., DIADEM)
- Analystical processing of structured data bases (e.g., legal conformance checks in health care)

Typical system requirements:

- Interactive or batch processing, depending on use case
- Data-related extensions (datatypes, built-ins, aggregation)
- Possibly domain-specific, structured datatypes

What is it good for? (3)

Application Area 3: Data Extraction and Transformation

Datalog allows us to define recursive views over large data collections:

- Rule-based relational DB data access (e.g., Yedalog, Logica)
- Rule-based graph DB data access (e.g., RDFox, Nemo)

Typical system requirements:

- Mostly interactive query answering
- Database bindings and matching datatypes
- Efficient update handling

What is it good for? (4)

Application Area 4: Graph and Network Analysis

Graph-like structures suggest iterative, declarative processing:

- Network analysis, e.g., PageRank centrality (e.g., EmptyHeaded, SocialLite)
- Graph algorithms, e.g., shortest path (e.g., SocialLite, Dynalog)

Typical system requirements:

- Mostly main-memory based, may or may not be batch processed
- Custom control for termination of approxiation algorithms
- Support for recursive use of aggretation (at least min and max)

Semantics of Datalog

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Definition 7.4: Consider a database \mathcal{D} and a Datalog rule ρ of the form $H \leftarrow B_1, \ldots, B_n$. A ground substitution σ is a match for ρ on \mathcal{D} if (1) σ is defined exactly on the variables in ρ , and (2) $B_1\sigma, \ldots, B_n\sigma \in \mathcal{D}$. In this case, applying ρ to \mathcal{D} under σ yields the inference $H\sigma$.

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The output of a program are the facts that follow by applying rules exhaustively.

The Consequence Operator

Definition 7.5: The immediate consequence operator T_P maps sets of ground facts \mathcal{D} to sets of ground facts $T_P(\mathcal{D})$:

$$T_P(\mathcal{D}) = \{H\sigma \mid \text{there is some } H \leftarrow B_1, \dots, B_n \in P \text{ with match } \sigma \text{ on } \mathcal{D}\}$$

Given a database \mathcal{D} , we can define a sequence of databases \mathcal{D}_{P}^{i} as follows:

$$\mathcal{D}_P^0 = \mathcal{D} \qquad \mathcal{D}_P^{i+1} = \mathcal{D} \cup T_P(\mathcal{D}_P^i) \qquad \mathcal{D}_P^\infty = \bigcup_{i \geq 0} \mathcal{D}_P^i$$

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Observations:

- We obtain an increasing sequence $\mathcal{D}_P^0 \subseteq \mathcal{D}_P^1 \subseteq \mathcal{D}_P^2 \subseteq \ldots \subseteq \mathcal{D}_P^\infty$ (why?)
- Only a finite number of ground facts can ever be derived from $\mathcal{D} \cup P$ (why?).
- Hence the sequence $\mathcal{D}_{P}^{0}, \mathcal{D}_{P}^{1}, \dots$ is finite and there is some $k \geq 1$ with $\mathcal{D}_{P}^{k} = \mathcal{D}_{P}^{\infty}$.

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Definition 7.6: The output database of P over \mathcal{D} is the restriction of \mathcal{D}_{P}^{∞} to output predicates, i.e., the set $\{p(c_{1},\ldots,c_{n})\mid p(c_{1},\ldots,c_{n})\in\mathcal{D}_{P}^{\infty},p\in\mathbf{P}_{\text{out}}\}.$

The consequence operator: Example

Datalog rules P:

```
\begin{aligned} \mathsf{parent}(x,y) &\leftarrow \mathsf{father}(x,y) \\ \mathsf{parent}(x,y) &\leftarrow \mathsf{mother}(x,y) \\ \mathsf{ancestor}(x,y) &\leftarrow \mathsf{parent}(x,y) \\ \mathsf{ancestor}(x,z) &\leftarrow \mathsf{ancestor}(x,y), \mathsf{parent}(y,z) \\ \mathsf{commonAnc}(x) &\leftarrow \mathsf{ancestor}(\mathsf{alice},x), \mathsf{ancestor}(\mathsf{finley},x) \end{aligned}
```

Input database \mathcal{D} :

```
father(alice, bob)
mother(alice, cho)
mother(cho, eiko)
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```

```
 \mathcal{D}_{P}^{0} = \{ \text{father}(\text{alice}, \text{bob}), \text{mother}(\text{alice}, \text{cho}), \text{mother}(\text{cho}, \text{eiko}), \text{mother}(\text{finley}, \text{eiko}) \}   \mathcal{D}_{P}^{1} = \mathcal{D}_{P}^{0} \cup \{ \text{parent}(\text{alice}, \text{bob}), \text{parent}(\text{alice}, \text{cho}), \text{parent}(\text{cho}, \text{eiko}), \text{parent}(\text{finley}, \text{eiko}) \}   \mathcal{D}_{P}^{2} = \mathcal{D}_{P}^{1} \cup \{ \text{ancestor}(\text{alice}, \text{bob}), \text{ancestor}(\text{alice}, \text{cho}), \text{ancestor}(\text{cho}, \text{eiko}), \text{ancestor}(\text{finley}, \text{eiko}) \}   \mathcal{D}_{P}^{3} = \mathcal{D}_{P}^{2} \cup \{ \text{ancestor}(\text{alice}, \text{eiko}) \}   \mathcal{D}_{P}^{4} = \mathcal{D}_{P}^{3} \cup \{ \text{commonAnc}(\text{eiko}) \}   \mathcal{D}_{P}^{5} = \mathcal{D}_{P}^{4} = \mathcal{D}_{P}^{\infty}
```

Models of Datalog

Definition 7.7: An Herbrand model of P and \mathcal{D} is a database \mathcal{H} such that

- 1. $\mathcal{D} \subseteq \mathcal{H}$, and
- 2. for every rule $\rho \in P$ of the form $H \leftarrow B_1, \dots, B_n$, and every match σ for ρ over \mathcal{H} , we also have $H\sigma \in \mathcal{H}$.

Notes:

- Herbrand models interpret constants "as themselves", hence can be defined as sets of facts.
- Among all Herbrand models of P and \mathcal{D} , there is actually a least one (w.r.t. \subseteq), which coincides with \mathcal{D}_{P}^{∞} .

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Theorem 7.8: The output database of P over \mathcal{D} is equal to:

- the set of all output facts that are true in \mathcal{D}_{P}^{∞} ,
- the set of all output facts that are true in all Herbrand models of P and \mathcal{D} ,
- the set of all output facts that are true in all first-order models of P and \mathcal{D} .

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Proof trees

Definition 7.9: Consider a Datalog program P with input database \mathcal{D} . A proof tree with respect to P and \mathcal{D} is a tree structure T that satisfies the following conditions:

- 1. every node n of T is labelled by a fact $\lambda(n)$,
- 2. if *n* is a leaf node, then $\lambda(n) \in \mathcal{D}$,
- 3. if n is an inner node, then n is additionally labelled by a rule $H \leftarrow B_1, \ldots, B_k \in P$ and a substitution σ , such that (1) $\lambda(n) = H\sigma$ and (2) n has exactly k child nodes c_1, \ldots, c_k with $\lambda(c_i) = B_i\sigma$ for all $1 \le i \le k$.

If a proof tree T has root node r, we say that T is a proof for $\lambda(r)$ with respect to P and \mathcal{D} .

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Proof trees

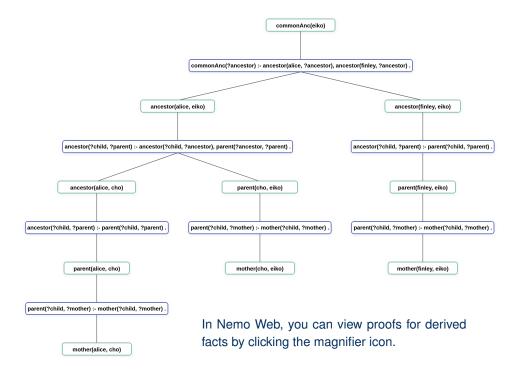
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If a proof tree T has root node r, we say that T is a proof for $\lambda(r)$ with respect to P and \mathcal{D} .

Theorem 7.10: The output database of P over \mathcal{D} is equal to the set of all ground facts for which there is a proof with respect to P and \mathcal{D} .

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Datalog as Second-Order Logic

Example 7.11: The following two programs are equivalent:

```
\begin{aligned} \operatorname{reach}(x,y) &\leftarrow \operatorname{edge}(x,y) & \operatorname{output}(y) \leftarrow \operatorname{edge}(c,y) \\ \operatorname{reach}(x,z) &\leftarrow \operatorname{reach}(x,y), \operatorname{reach}(y,z) & \operatorname{output}(z) \leftarrow \operatorname{output}(y), \operatorname{edge}(y,z) \\ \operatorname{output}(z) &\leftarrow \operatorname{reach}(c,z) \end{aligned}
```

Yet they do not have the same T_P operator, Herbrand models, or proof trees.

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```

Yet they do not have the same T_P operator, Herbrand models, or proof trees.

The following second-order logic formula captures the semantics more acurately:

$$\begin{array}{ll} \forall \ \mathsf{Reach}, \\ \mathsf{Output}. \end{array} \left(\left(\begin{array}{cc} (\ \forall x,y. & \mathsf{edge}(x,y)) \to \mathsf{Reach}(x,y)) \land \\ (\forall x,y,z. \ \mathsf{Reach}(x,y) \land \mathsf{Reach}(y,z) \to \mathsf{Reach}(x,z)) \land \\ (\ \forall z. & \mathsf{Reach}(c,z) \to \mathsf{Output}(z)) \end{array} \right) \to \mathsf{Output}(v) \\ \end{array} \right)$$

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Datalog Semantics: Summary

There are four equivalent ways of defining Datalog semantics:

- Operational semantics: least fixed point of consequence operator T_P
- Model-theoretic semantics: entailments of all/least Herbrand/FO model(s)
- Proof-theoretic semantics: every conclusion of some proof tree
- Second-order axiomatisation: Satisfying assignments in SO model checking

 \sim pleasing and reassuring agreement of various ideas, witnessing the underlying mathematical elegance

Note: Datalog is generally considered a fragment of second-order logic, but for most uses, we don't need to worry.

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Working with Real Data

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Using Datalog on RDF

Datalog assumes that databases are given as sets of (relational) facts.

How to apply Datalog to graph data?

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Using Datalog on RDF

Datalog assumes that databases are given as sets of (relational) facts.

How to apply Datalog to graph data?

Option 1: Properties as binary predicates

- An RDF triple s p o can be represented by a fact p(s, o)
- Both predicate names and constants are IRIs
- Datalog "sees" no relation between properties (predicates) and IRIs in subject and object positions

Option 2: Triples as ternary hyperedges

- An RDF triple s p o can be represented by a fact triple (s, p, o)
- triple is the only predicate needed to represent arbitrary databases
- IRIs on any triple position can be related in Datalog

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Where can input data come from?

We often want to use input databases that are not given as facts in the program:

- Scalability: Other formats are more suitable for large datasets
- Practicality: We don't want to edit our programs to change data
- Access: Some data sources cannot be converted to facts (size, access restrictions, legal constraints)

→ many systems support data imports

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- → many systems support data imports

Commonly supported data sources include:

- CSV/TSV/DSV files: simple relational text format
- RDF: knowledge graphs in triples and quads
- SQL bindings: loading directly from relational DBMS
- SPARQL bindings: loading directly from RDF database

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Data inputs in Nemo

Nemo supports CSV/TSV/DSV, RDF, and SPARQL

- RDF imports: Nemo can import triple data from all standard formats; imported triples are stored in a ternary predicate; a file path or URL needs to be specified
- SPARQL imports: Nemo can import query results of arbitrary SPARQL queries into
 predicates of suitable arity (depending on number of selected variables); a query service
 (endpoint) needs to be specified with the query

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A Worked Example: https://tud.link/wkrajt

```
% Prefixes help to abbreviate long identifiers or URLs:
    @prefix wdgs: <https://guerv.wikidata.org/> .
    @prefix wd: <http://www.wikidata.org/entity/> .
    % Parameters can be used for fixed terms throughout the program:
    @parameter $personId1 = wd:07259 . % Ada Lovelace
    @parameter $personId2 = wd:014045 . % Mobv
    % Import predicate "wdParent" (mother or father) through SPARQL:
    @import wdParent :- spargl{
      endpoint=wdqs:sparql,
10
11
      query="""PREFIX wdt: <http://www.wikidata.org/prop/direct/>
        SELECT ?child ?parent WHERE { ?child (wdt:P22|wdt:P25) ?parent }"""
13
    % Import predicate "wdLabel" (English label) through SPARQL:
    @import wdLabel :- sparql{
15
      endpoint=wdgs:spargl.
16
17
      query="""PREFIX wikibase: <http://wikiba.se/ontology#>
18
        SELECT ?qid ?qidLabel WHERE {
          SERVICE wikibase: label {
20
            <http://www.biqdata.com/rdf#serviceParam> wikibase:language "mul,en" } }"""
21
    } .
    % Find relevant ancestors, starting from selected persons:
24
    ancestor($personId1, ?parent) :- wdParent($personId1, ?parent) .
    ancestor($personId2. ?parent) :- wdParent($personId2. ?parent) .
     ancestor(?person, ?ancestor) :- ancestor(?person, ?x), wdParent(?x, ?ancestor) .
26
    % Find common ancestors, and determine their names:
28
    commonAnc(?qid, ?name) :- ancestor($personId1, ?qid), ancestor($personId2, ?qid),
                              wdLabel(?gid.?name) .
    % Select one output predicate:
    @output commonAnc .
```

Summary

Pure Datalog is an elegant and simple rule language

Datalog smoothly works with diverse data formats, including knowledge graphs

Datalog has a declarative, logic-based semantics, and this has important practical benefits

What's next?

- More features of Datalog
- Complexity and Expressivity of SPARQL and Datalog
- Ontology languages

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References

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